

The Future of Deep Learning: Deep Generative Modeling

Jakub Tomczak

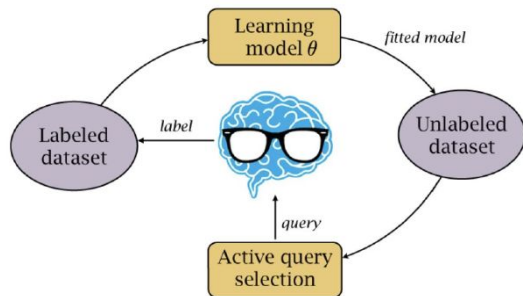
Amsterdam, April 5, 2019

Applications of Deep Learning

“ i want to talk to you . ”
“ i want to be with you . ”
“ i do n't want to be with you . ”
i do n't want to be with you .
she did n't want to be with him .

he was silent for a long moment .
he was silent for a moment .
it was quiet for a moment .
it was dark and cold .
there was a pause .
it was my turn .

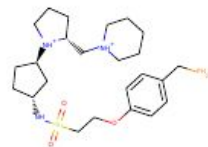
Text analysis



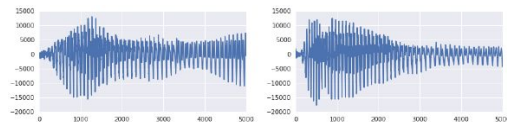
Active Learning



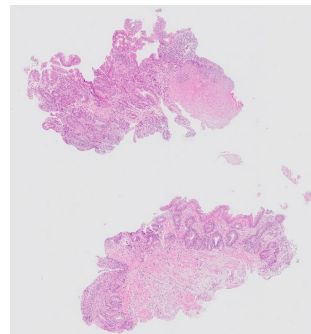
Image analysis



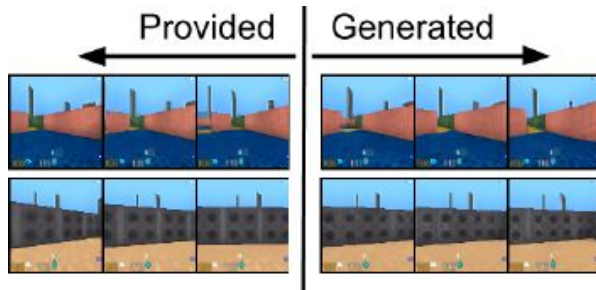
Graph analysis



Audio analysis



Medical data



Reinforcement Learning

and more...

Is generative modeling important?

We learn a neural network to classify images:



Is generative modeling important?

We learn a neural network to classify images:



$p(\mathbf{panda}|x)=0.99$

...

Is generative modeling important?

We learn a neural network to classify images:



+




$p(\text{panda}|x)=0.99$

noise

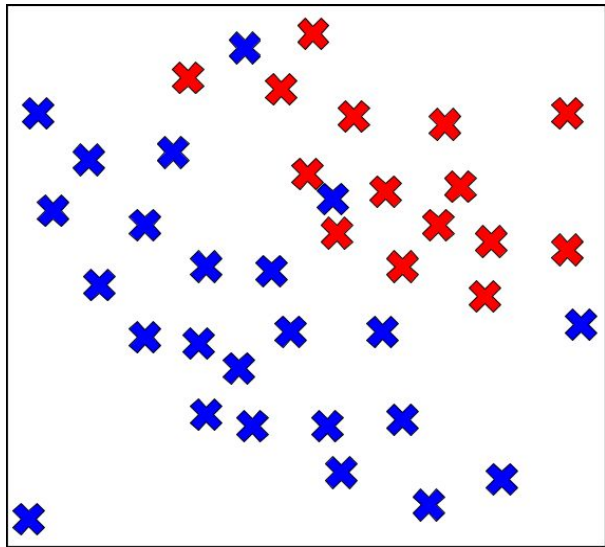
...

Is generative modeling important?

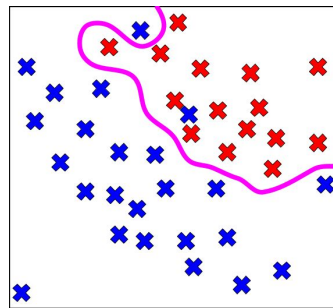
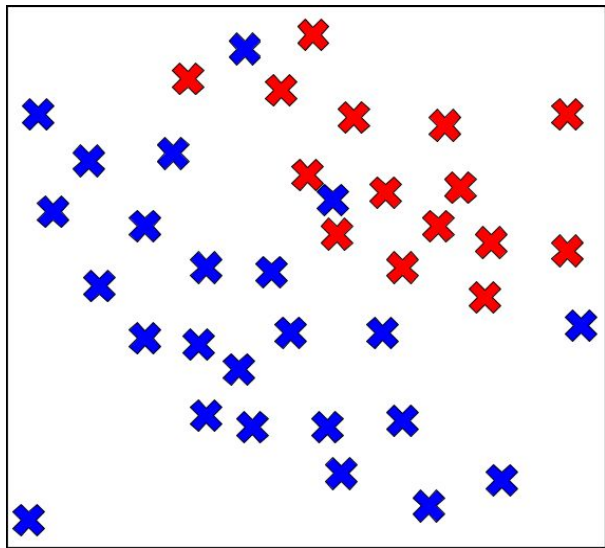
We learn a neural network to classify images:


$$\begin{array}{ccc} \text{panda} & + & \text{noise} & = & \text{panda} \\ p(\mathbf{panda}|x)=0.99 & & \text{noise} & & p(\mathbf{panda}|x)=0.01 \\ \dots & & & & \dots \\ & & & & p(\mathbf{monkey}|x)=0.9 \end{array}$$

Is generative modeling important?

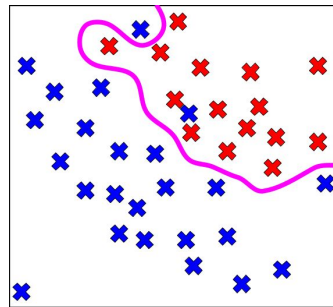
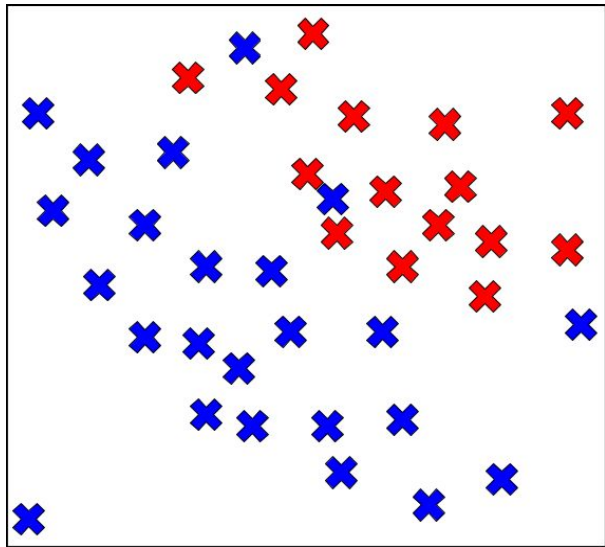


Is generative modeling important?

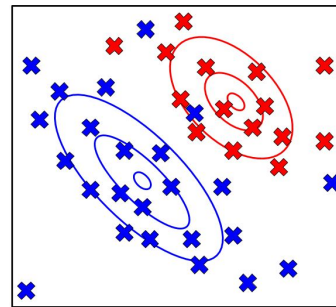


$$p_{\theta}(y|x)$$

Is generative modeling important?



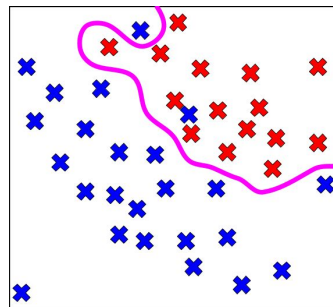
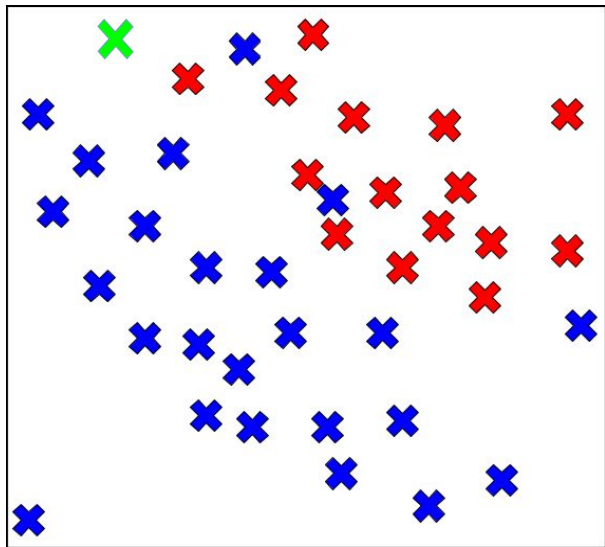
$$p_{\theta}(y|x)$$



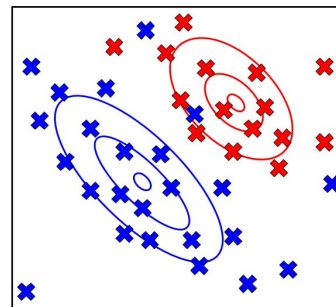
$$p_{\theta}(x, y) = p_{\theta}(y|x) p_{\theta}(x)$$

Is generative modeling important?

new data



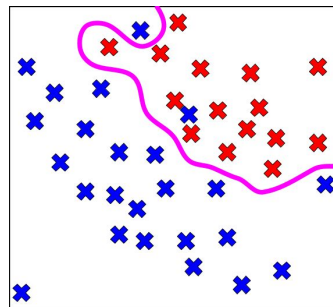
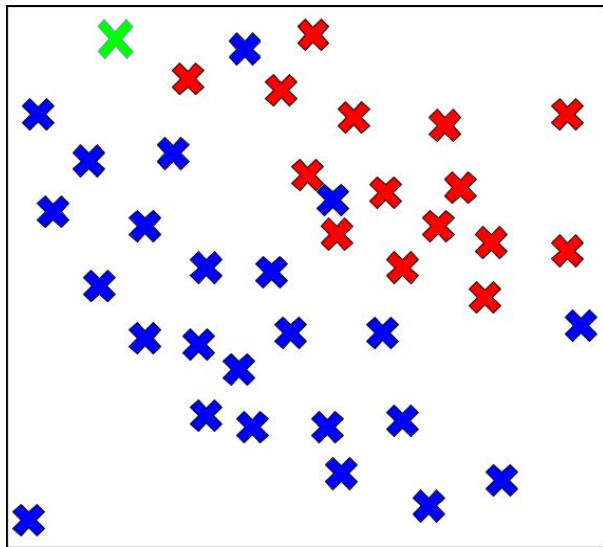
$$p_{\theta}(y|x)$$



$$p_{\theta}(x, y) = p_{\theta}(y|x) p_{\theta}(x)$$

Is generative modeling important?

new data

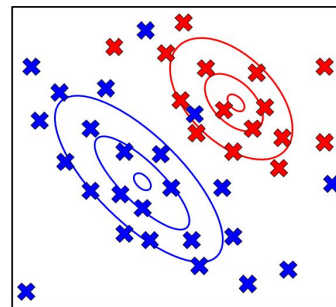


$$p_{\theta}(y|x)$$

High probability
of the **blue** label.

=

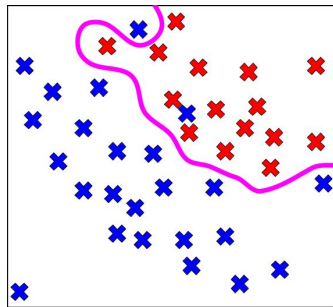
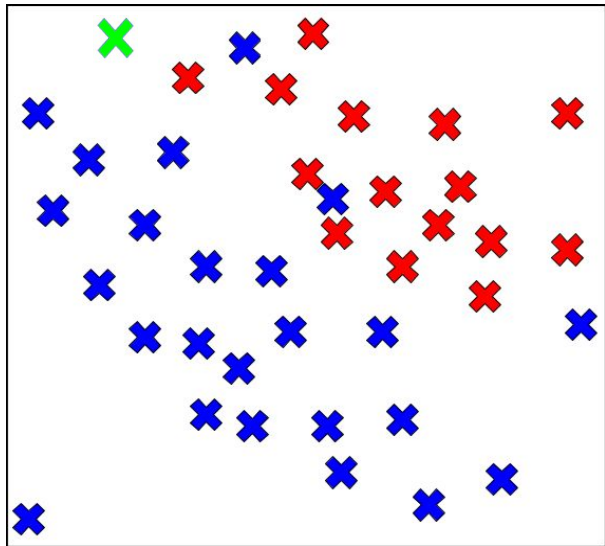
**Highly probable
decision!**



$$p_{\theta}(x, y) = p_{\theta}(y|x) p_{\theta}(x)$$

Is generative modeling important?

new data

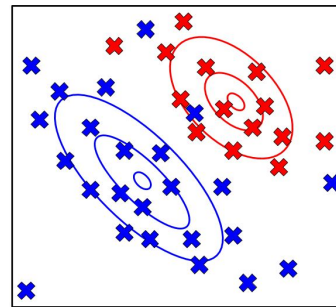


$$p_{\theta}(y|x)$$

High probability
of the **blue** label.

=

Highly probable
decision!



$$p_{\theta}(x, y) = p_{\theta}(y|x) p_{\theta}(x)$$

High probability
of the **blue** label.

x

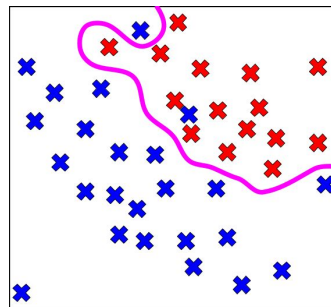
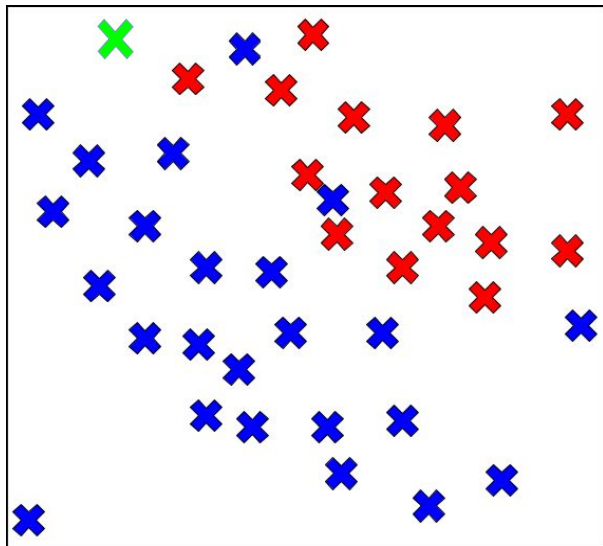
Low probability
of the **object**

=

Uncertain
decision!

Is generative modeling important?

new data

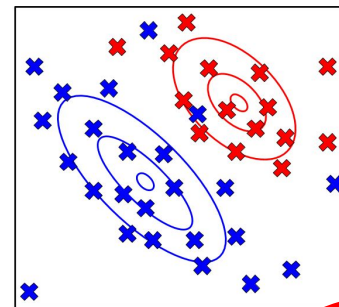


$$p_{\theta}(y|x)$$

High probability
of the **blue** label.

=

Highly probable
decision!



$$p_{\theta}(x, y) = p_{\theta}(y|x) p_{\theta}(x)$$

High probability
of the **blue** label.

x

Low probability
of the **object**

=

Uncertain
decision!



What is generative modeling about?

Understanding:

$$p(y, \mathbf{x}) = p(y|\mathbf{x}) p(\mathbf{x})$$

finding underlying
factors (**discovery**)

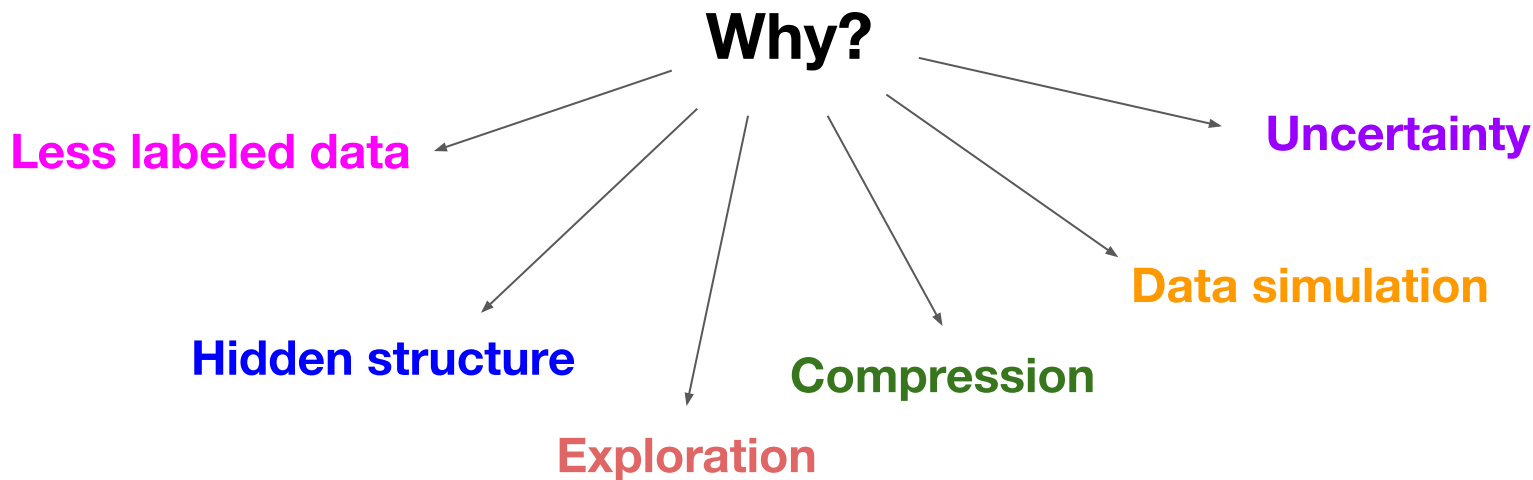
predicting and
anticipating future
events (**planning**)

finding analogies
(**transfer learning**)

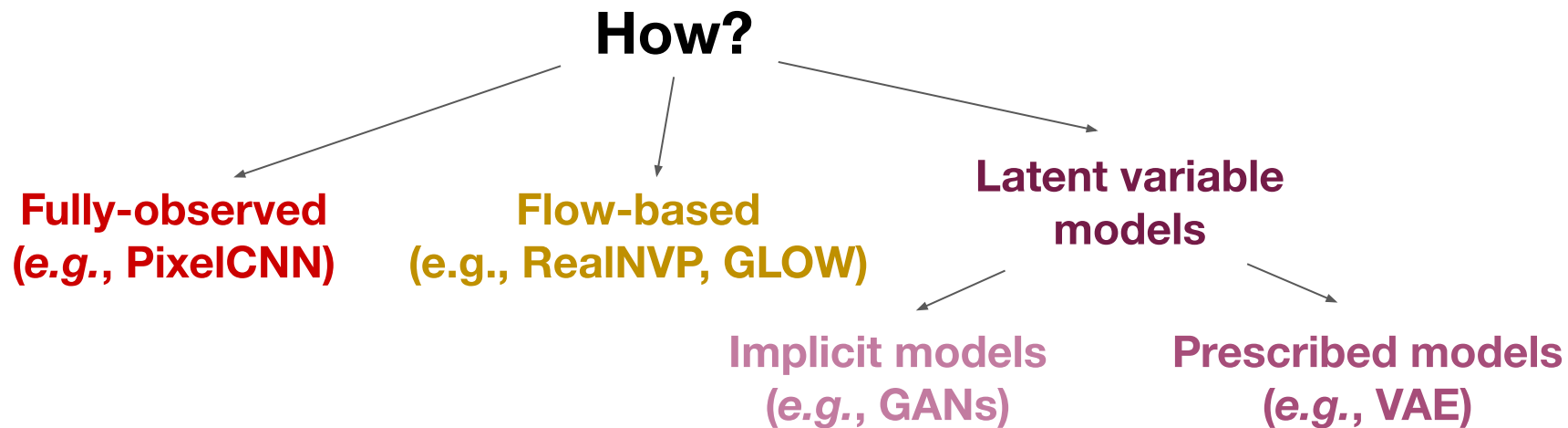
detecting rare events
(**anomaly detection**)

decision making

Why generative modeling?



Generative modeling: **How?**

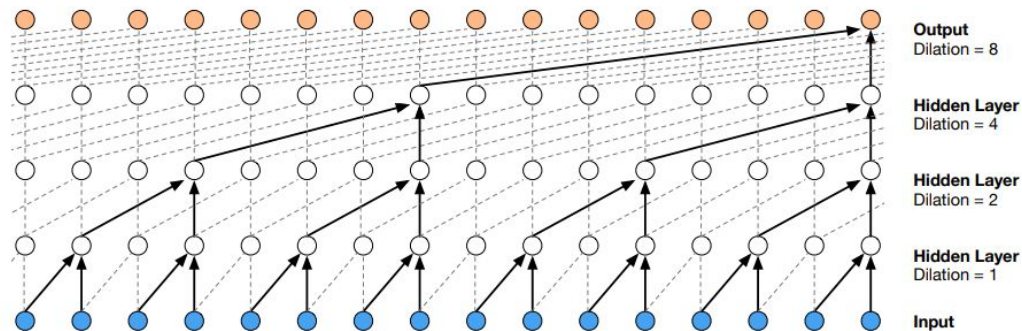


Generative modeling: **Auto-regressive models**

General idea is to factorise the joint distribution:

$$p(\mathbf{x}) = p(x_1) \prod_{d=2}^D p(x_d | \mathbf{x}_{1:d-1})$$

and use neural networks (e.g., convolutional NN) to model it efficiently:

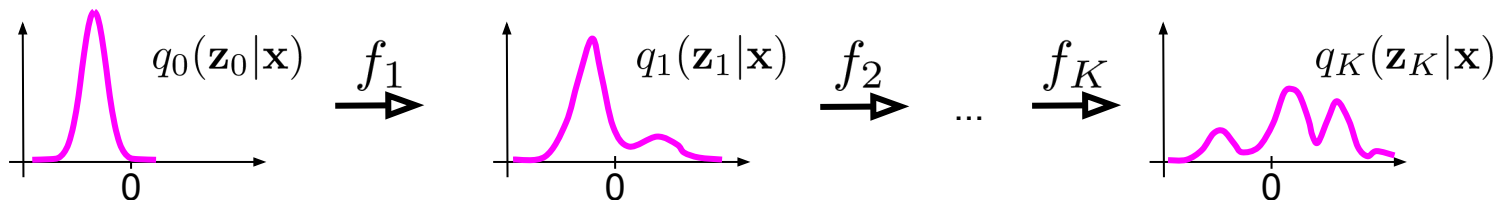


Generative modeling: **Flow-based models**

- Sample from a “simple” distribution:

$$\mathbf{z}_0 \sim q_0(\mathbf{z}|\mathbf{x}) = \mathcal{N}(\mathbf{z}|\mu(\mathbf{x}), \text{diag}(\sigma^2(\mathbf{x})))$$

- Apply a sequence of K **invertible** transformations: $f_k : \mathbb{R}^M \rightarrow \mathbb{R}^M$



and the change of variables yields:

$$q_K(\mathbf{z}_K|\mathbf{x}) = q_0(\mathbf{z}_0|\mathbf{x}) \prod_{k=1}^K \left| \det \frac{\partial f_k(\mathbf{z}_{k-1})}{\partial \mathbf{z}_{k-1}} \right|^{-1}$$

Generative modeling: **Latent Variable Models**

We assume data lies on a low-dimensional manifold so the generator is:

$$\mathbf{x} = f_{\theta}(\mathbf{z})$$

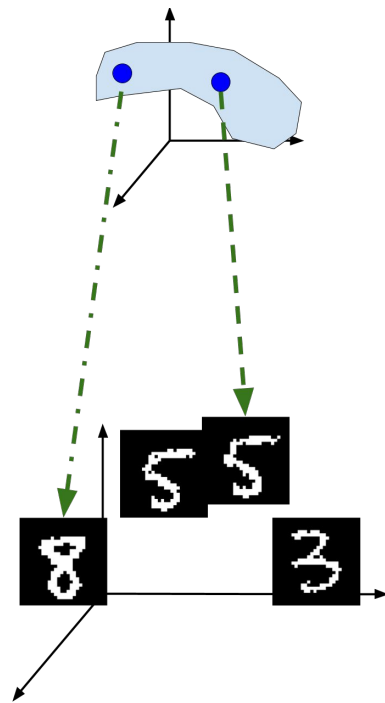
where:

$$\mathbf{x} \in \mathcal{X} \text{ (e.g. } \mathcal{X} = \mathbb{R}^D \text{) and } \mathbf{z} \in \mathbb{R}^d$$

Two main approaches:

→ **Generative Adversarial Networks** (GANs)

→ **Variational Auto-Encoders** (VAEs)



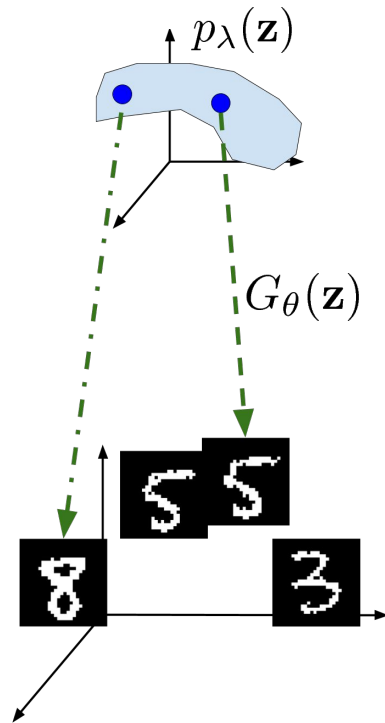
Generative modeling: **GANs**

We assume a **deterministic generator**:

$$\mathbf{x} = G_{\theta}(\mathbf{z})$$

and **a prior** over latent space:

$$\mathbf{z} \sim p_{\lambda}(\mathbf{z})$$



Generative modeling: **GANs**

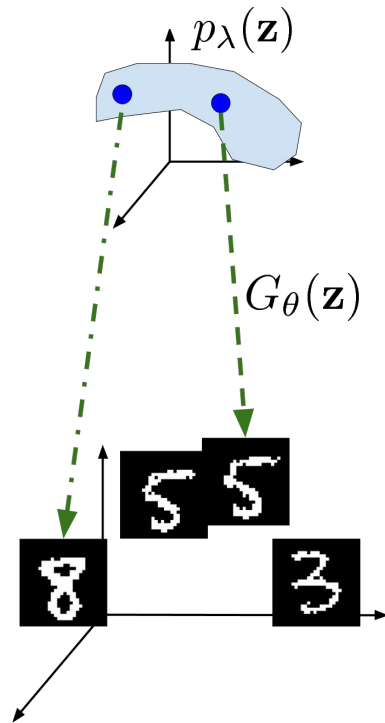
We assume a **deterministic generator**:

$$\mathbf{x} = G_{\theta}(\mathbf{z})$$

and **a prior** over latent space:

$$\mathbf{z} \sim p_{\lambda}(\mathbf{z})$$

How to train it?



Generative modeling: **GANs**

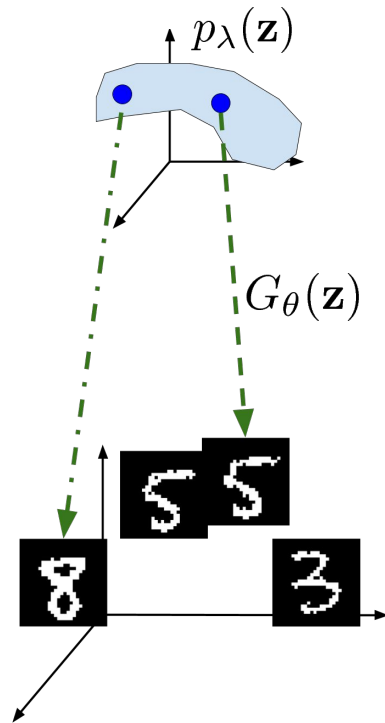
We assume a **deterministic generator**:

$$\mathbf{x} = G_{\theta}(\mathbf{z})$$

and **a prior** over latent space:

$$\mathbf{z} \sim p_{\lambda}(\mathbf{z})$$

How to train it? By using a game!



Generative modeling: **GANs**

We assume a **deterministic generator**:

$$\mathbf{x} = G_{\theta}(\mathbf{z})$$

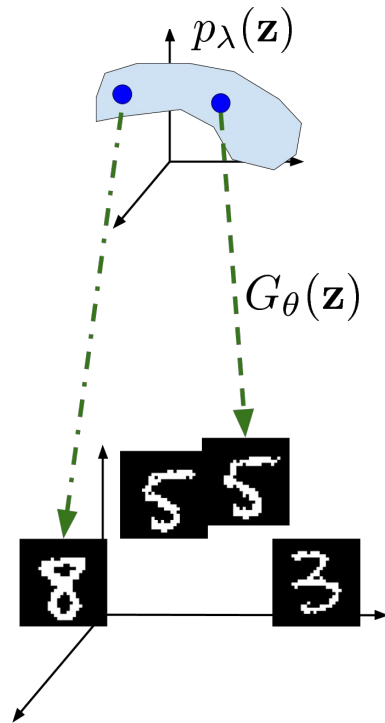
and **a prior** over latent space:

$$\mathbf{z} \sim p_{\lambda}(\mathbf{z})$$

How to train it? By using a game!

For this purpose, we assume a discriminator:

$$D_{\psi}(\mathbf{x}) \in [0, 1]$$



Generative modeling: GANs

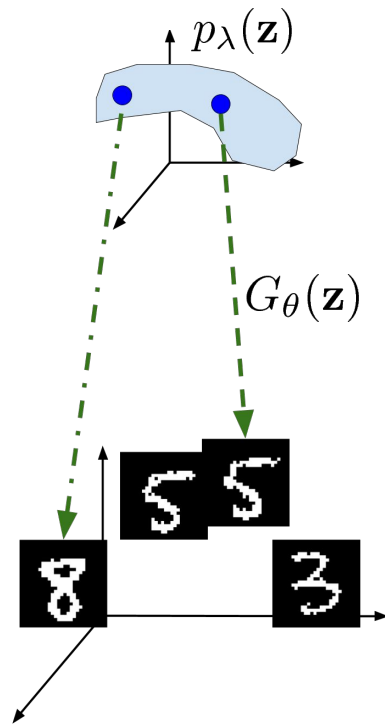
The learning process is as follows:

- the **generator** tries to **fool** the **discriminator**;
- the **discriminator** tries to **distinguish** between the **real** and **fake** images.

We define the learning problem as a min-max problem:

$$\min_{\theta} \max_{\psi} \mathbb{E}_{\mathbf{x} \sim p_{data}} \left[\ln D_{\psi}(\mathbf{x}) \right] - \mathbb{E}_{\mathbf{z} \sim p_{\lambda}(\mathbf{z})} \left[\ln (1 - D_{\psi}(G(\mathbf{z}))) \right]$$

In fact, we have a **learnable loss** function!



Generative modeling: GANs

The learning process is as follows:

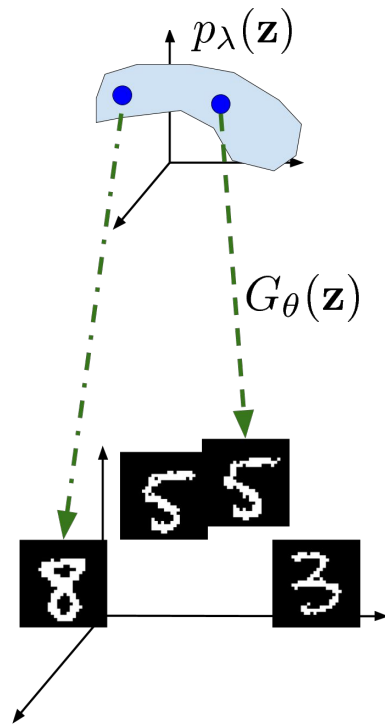
- the **generator** tries to **fool** the **discriminator**;
- the **discriminator** tries to **distinguish** between the **real** and **fake** images.

We define the learning problem as a min-max problem:

$$\min_{\theta} \max_{\psi} \mathbb{E}_{\mathbf{x} \sim p_{data}} \left[\ln D_{\psi}(\mathbf{x}) \right] - \mathbb{E}_{\mathbf{z} \sim p_{\lambda}(\mathbf{z})} \left[\ln (1 - D_{\psi}(G(\mathbf{z}))) \right]$$

In fact, we have a **learnable loss** function!

→ It learns high-order statistics.



Generative modeling: **GANs**

Pros:

- we don't need to specify a likelihood function;
- very flexible;
- the loss function is trainable;
- perfect for data simulation.

Cons:

- we don't know the distribution;
- training is highly unstable (min-max objective);
- missing mode problem.

Generative modeling: **VAEs**

We assume **a stochastic generator** (decoder) and a **prior**:

$$\mathbf{z} \sim p_{\lambda}(\mathbf{z})$$

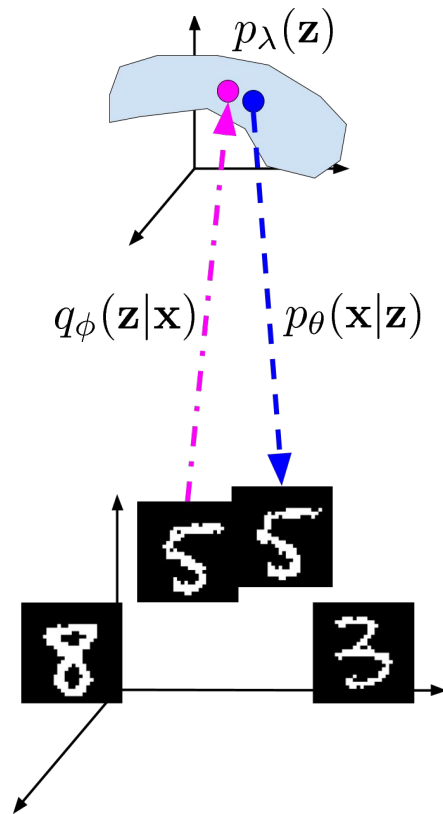
$$\mathbf{x} \sim p_{\theta}(\mathbf{x}|\mathbf{z})$$

Additionally, we use **a variational posterior** (encoder):

$$\mathbf{z} \sim q_{\phi}(\mathbf{z}|\mathbf{x})$$

How to train it? Using the log-likelihood function!

$$\ln p(\mathbf{x}) \geq \mathbb{E}_{\mathbf{z} \sim q_{\phi}(\mathbf{z}|\mathbf{x})} \left[\ln p_{\theta}(\mathbf{x}|\mathbf{z}) \right] - \text{KL} \left[q_{\phi}(\mathbf{z}|\mathbf{x}) || p_{\lambda}(\mathbf{z}) \right]$$



Variational Auto-Encoder: Extensions

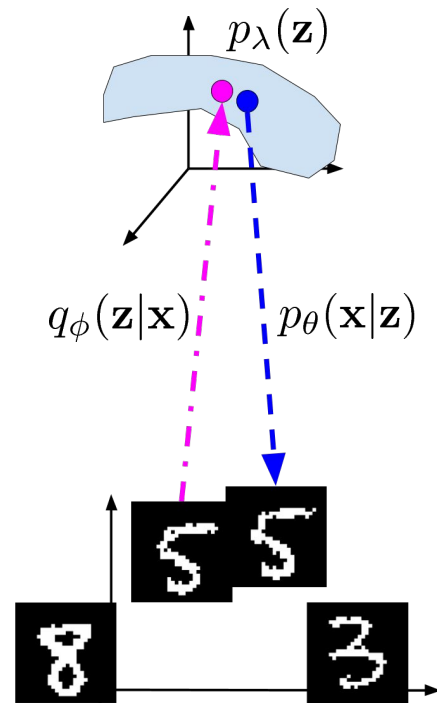
$$q_{\phi}(\mathbf{z}|\mathbf{x}) \propto p_{\theta}(\mathbf{x}|\mathbf{z}) p_{\lambda}(\mathbf{z})$$

Normalizing flows
Volume-preserving flows
non-Gaussian distributions

Fully-connected
ConvNets
PixelCNN
Other

Importance Weighted AE
Renyi Divergence
Stein Divergence

Autoregressive Prior
Objective Prior
Stick-Breaking Prior
VampPrior



- Tomczak, J. M., & Welling, M. (2016). Improving variational auto-encoders using householder flow. *NIPS Workshop 2016*.
Berg, R. V. D., Hasenclever, L., Tomczak, J. M., & Welling, M. (2018). Sylvester Normalizing Flows for Variational Inference. *UAI 2018*.
Tomczak, J. M., & Welling, M. (2017). VAE with a VampPrior. *arXiv preprint arXiv:1705.07120*. (AISTATS 2018)
Davidson, T. R., Falorsi, L., De Cao, N., Kipf, T., & Tomczak, J. M. (2018). Hyperspherical Variational Auto-Encoders. *UAI 2018*.

Generative modeling: **VAEs**

Pros:

- we know the distribution and can calculate the likelihood function;
- we can encode an object in a low-dim manifold (compression);
- training is stable;
- no missing modes.

Cons:

- we need know the distribution;
- we need a flexible encoder and prior;
- blurry images (so far...).

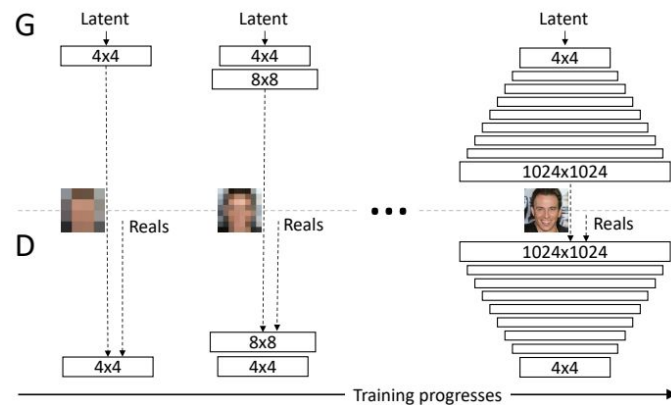
Recent successes: Image generation (GANs)



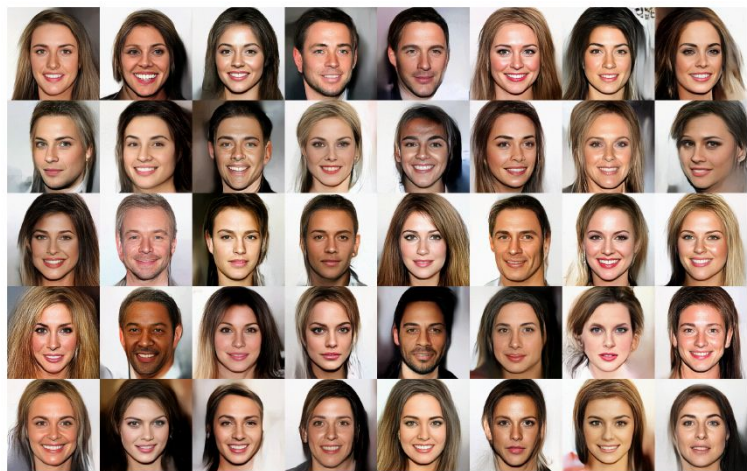
generated



real



Recent successes: Image generation (GLOW)



generations



interpolations



(a) Smiling

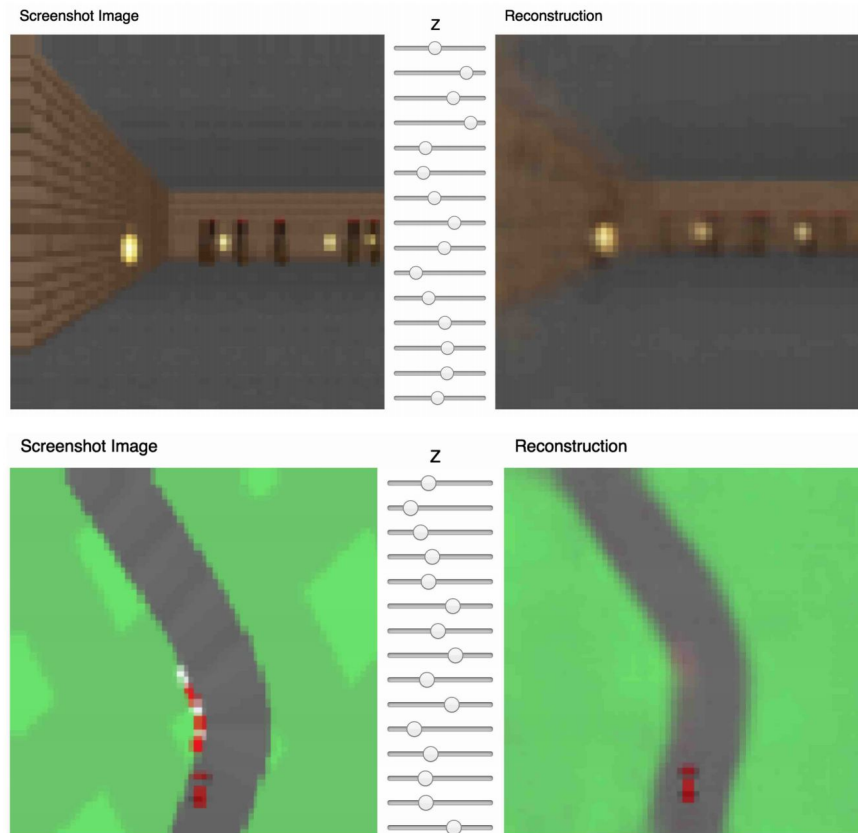
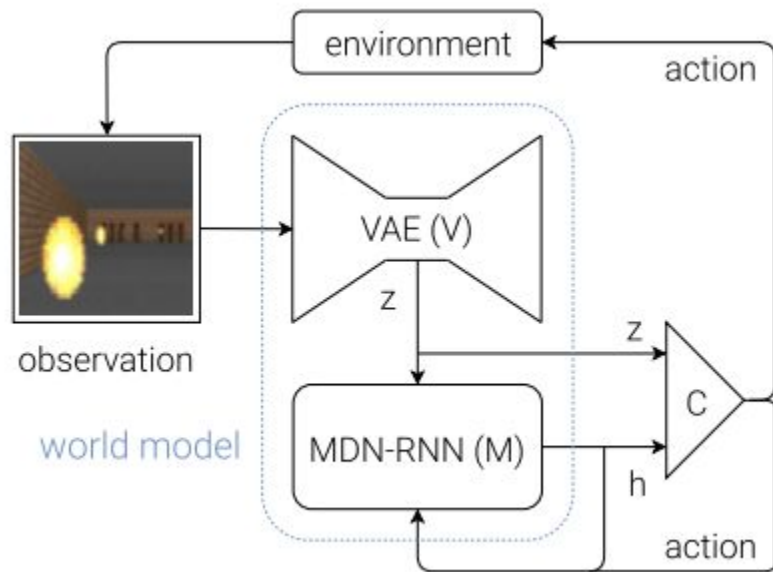
(b) Pale Skin



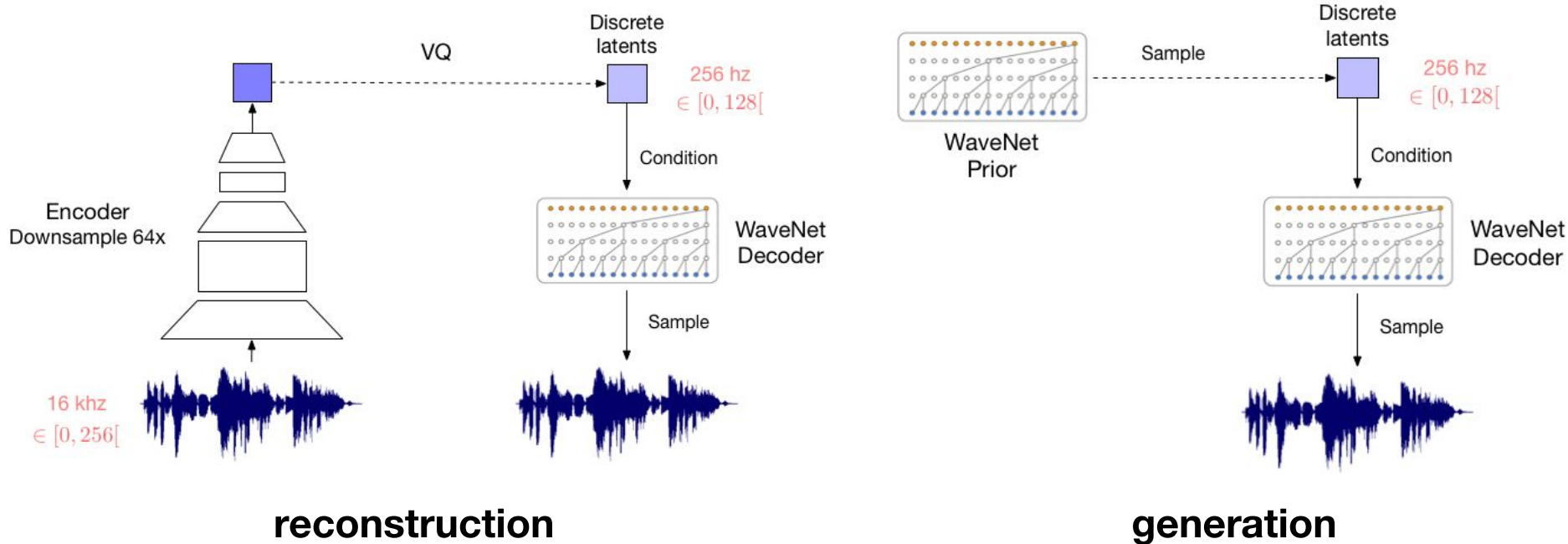
(c) Blond Hair

(d) Narrow Eyes

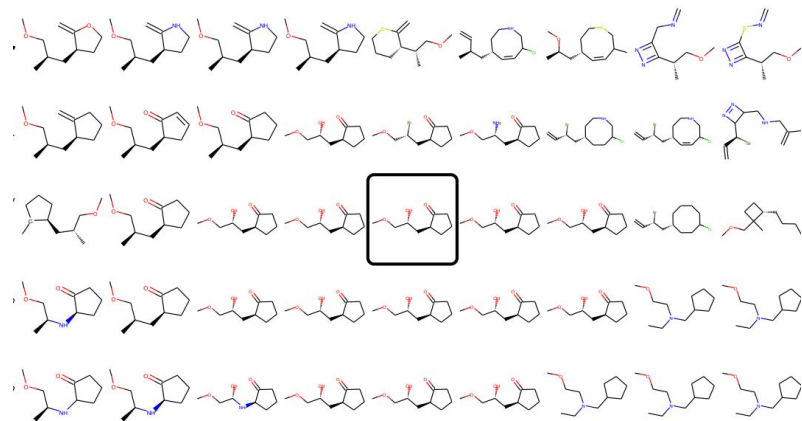
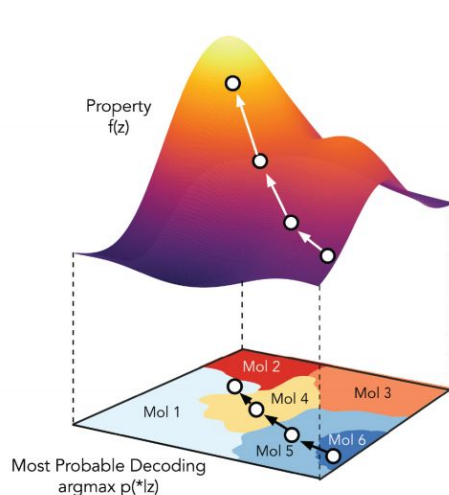
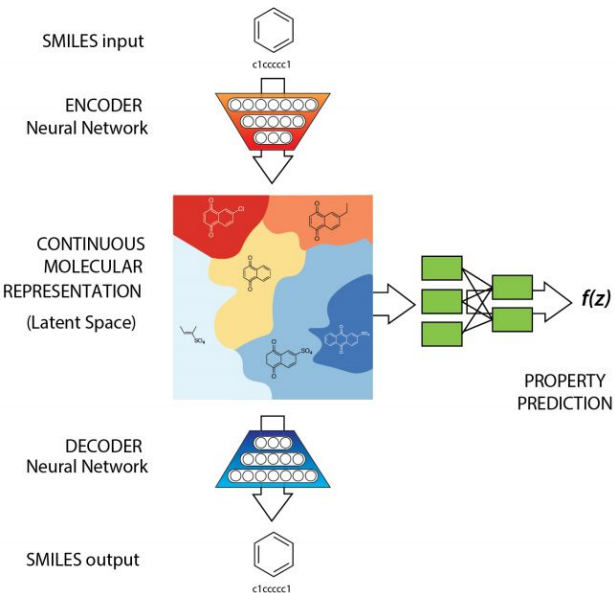
Recent successes: Reinforcement learning



Recent successes: **Audio generation**



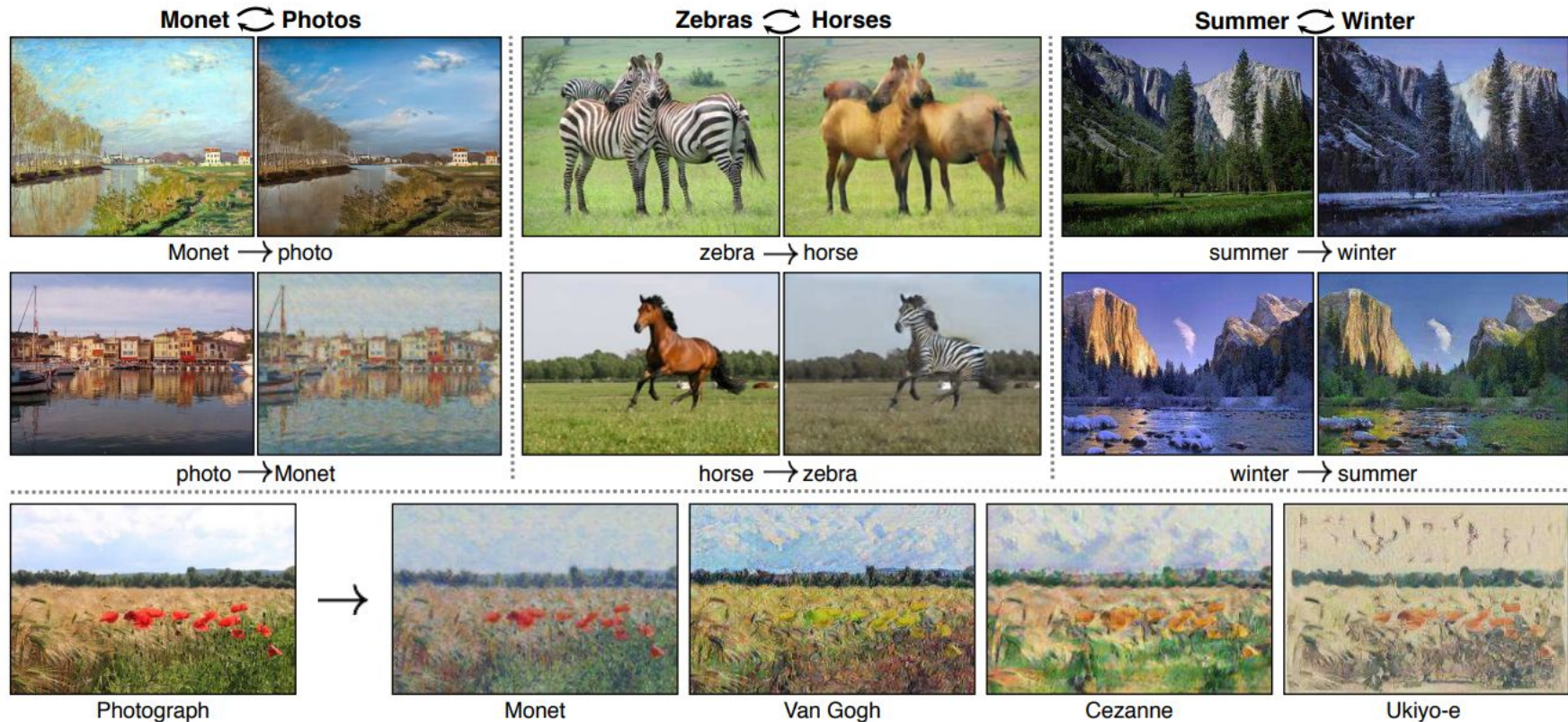
Recent successes: Drug discovery



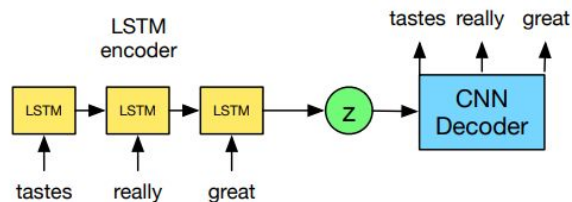
Gómez-Bombarelli, R., et al. (2018). Automatic Chemical Design Using a Data-Driven Continuous Representation of Molecules ACS Cent.

Kusner, M. J., Paige, B., & Hernández-Lobato, J. M. (2017). Grammar variational autoencoder. *arXiv preprint arXiv:1703.01925*.

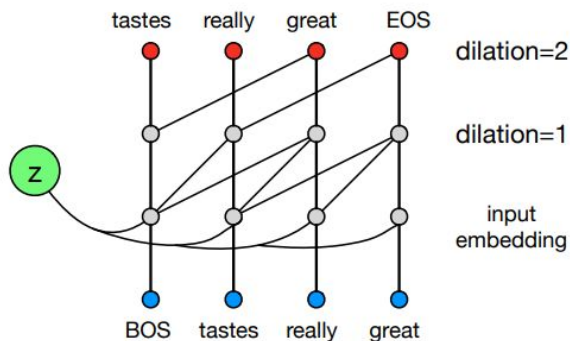
Recent successes: **Style transfer**



Recent successes: Text generation

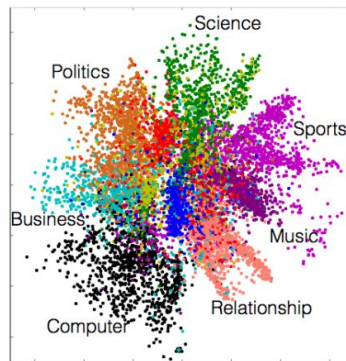


(a) VAE training graph using a dilated CNN decoder.

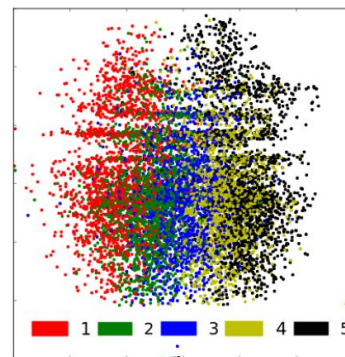


(b) Digram of dilated CNN decoder.

-
- | | |
|---------------|---|
| 1 star | the food was good but the service was horrible . took forever to get our food . we had to ask twice for our check after we got our food . will not return . |
| 2 star | the food was good , but the service was terrible . took forever to get someone to take our drink order . had to ask 3 times to get the check . food was ok , nothing to write about . |
| 3 star | came here for the first time last night . food was good . service was a little slow . food was just ok . |
| 4 star | food was good , service was a little slow , but the food was pretty good . i had the grilled chicken sandwich and it was really good . will definitely be back ! |
| 5 star | food was very good , service was fast and friendly . food was very good as well . will be back ! |
-

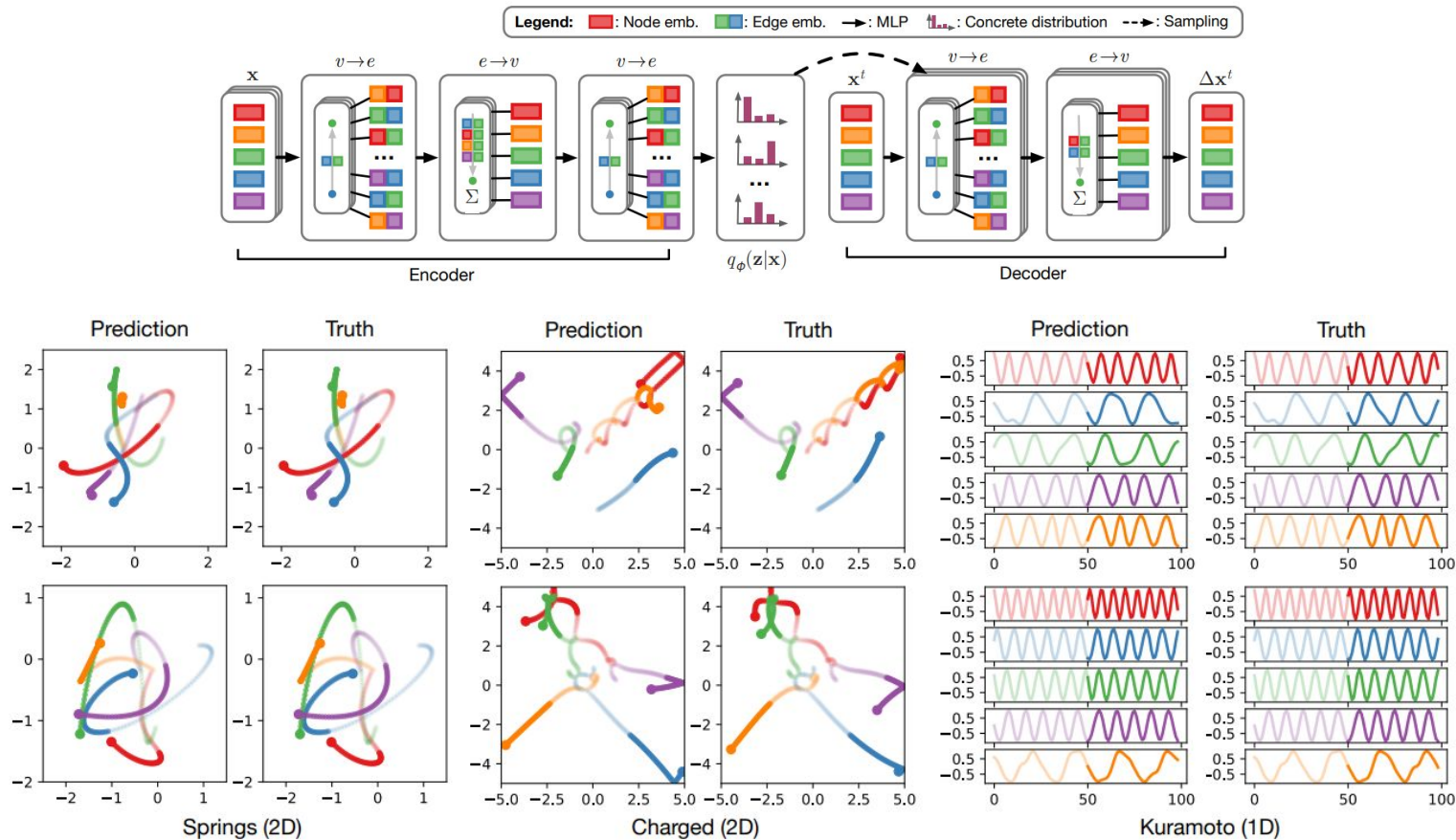


(a) Yahoo



(b) Yelp

Recent successes: Physics (interacting systems)



Conclusion



Generative modeling: the way to go to achieve AI.

Deep generative modeling: **very successful** in recent years in many domains.

GANs, VAEs,
Autoregressive models
and **Flow-based models**

Next steps: **video processing, better priors** and **decoders, geometric methods, ...**

Conclusion



Generative modeling: the way to go to achieve AI.

Deep generative modeling: **very successful** in recent years in many domains.


GANs, VAEs,
Autoregressive models
and **Flow-based models**

Next steps: **video processing, better priors and decoders, geometric methods, ...**

Conclusion




Generative modeling: the way to go to achieve AI.



Deep generative modeling: **very successful** in recent years in many domains.

GANs, VAEs,
Autoregressive models
and Flow-based models

Next steps: video
processing, better priors
and decoders, geometric
methods, ...



Conclusion

Generative modeling: the way to go to achieve AI.

Deep generative modeling: **very successful** in recent years in many domains.

GANs, **VAEs**,
Autoregressive models
and **Flow-based models**

Next steps: video processing, better priors and decoders, geometric methods, ...

Conclusion

Generative modeling: the way to go to achieve AI.

Deep generative modeling: **very successful** in recent years in many domains.

GANs, **VAEs**,
Autoregressive models
and **Flow-based models**

Next steps: **video processing**, **better priors** and **decoders**, **geometric methods**, ...

Code on github:

<https://github.com/jmtomczak>

Webpage:

<http://jmtomczak.github.io/>

Contact:

jmk.tomczak@gmail.com